WEEKLY SCHEDULE – TOPOLOGY OF MANIFOLDS – ETH ZÜRICH, SPRING 2022

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Lecture 1. – 20.02 – What is this course about?

 $\circ\,$ Definition of Top and Diff manifolds.

Key Thm 1. Diff and Top: Schoenflies Conjecture

Key Thm 2. Top: Poincaré Conjecture

Key Thm 3. Diff: exotic smooth structures

- Key Thm 0 [h-and s-cobordism Thms]: statements, ingredients
- $\circ\,$ orientations, tangent bundle

Lecture 2. -27.02 - Diff - Main tools

- vector fields, Thm: can find integral curves
- Collar Thm, Thm: no crit.pts implies product
- Thm: Handle Decomposition Thm
- submanifolds, transversality, isotopy, ambient isotopy,
- tubular neighbourhoods

Lecture 3. – **05.03** – Diff – Handle Calculus

- $\,\circ\,$ gluing, connected sum, handle attachment
- $\circ~$ examples of handle decompositions
- Isotopy Lemma, Unknot Lemma & Cor
- Reordering Lemma
- Cancellation Lemma
- $\circ\,$ Remove 0-handles Lemma