

C++11 code 11.7.13: Implementation of `slopelimfluxdiffper()` → [GitLab](#)

```
2 // Function parameters:
3 // double h: meshwidth of equidistant spatial grid
4 // Vector mu: (finite) vector  $\vec{\mu}$  of cell averages
5 // Functor F: 2-point numerical flux function  $F = F(v, w)$ 
6 // Functor slope: slope reconstruction function
7 //  $h\sigma_j = \text{slopes}(\mu_{j-1}, \mu_j, \mu_{j+1})$ 
8 //
9 // returns a vector with differences of numerical fluxes
10 //
11 // Function that realizes  $-h \cdot$  the right hand side operator
12 //  $\mathcal{L}_h$  for the method-of-lines ODE arising from conservative finite
13 // volume semidiscretization of the Cauchy problem for a 1D scalar
14 // conservation
15 // law [Lecture → Eq. (11.2.2.1)] in a 1-periodic setting.
16 template <typename FunctionF, typename FunctionSlopes>
17 Eigen::VectorXd slopelimfluxdiffper(const Eigen::VectorXd &mu, FunctionF &&F,
18                                     FunctionSlopes &&slopes) {
19     int n = mu.size(); // Number of active dual grid cells
20     Eigen::VectorXd sigma = Eigen::VectorXd::Zero(n); // Vector of slopes
21     Eigen::VectorXd fd = Eigen::VectorXd::Zero(n); // Flux differences
22
23     // Computation of slopes  $\sigma_j$ , uses  $\mu_{-1} = \mu_{n-1}$ ,
24     //  $\mu_n = \mu_0$ , which amounts to constant extension of states
25     // beyond domain of influence  $[a, b]$  of non-constant initial data. Same
26     // technique has been applied in [Lecture → Code 11.3.2.9]
27     sigma[0] = slopes(mu[n - 1], mu[0], mu[1]); // @@
28     for (int j = 1; j < n - 1; ++j)
29         sigma[j] = slopes(mu[j - 1], mu[j], mu[j + 1]);
30     sigma[n - 1] = slopes(mu[n - 2], mu[n - 1], mu[0]); // @@
31
32     // Compute linear reconstruction at endpoints of dual cells [Lecture →
33     // Eq. (11.5.1.2)]
34     Eigen::VectorXd nup = mu + 0.5 * sigma;
35     Eigen::VectorXd num = mu - 0.5 * sigma;
36
37     // Rely on periodicity to compute numerical fluxes at interval ends
38     fd[0] = F(nup[0], num[1]) - F(nup[n - 1], num[0]); // @@
39     for (int j = 1; j < n - 1; ++j)
40         // see [Lecture → Eq. (11.3.2.8)]
41         fd[j] = F(nup[j], num[j + 1]) - F(nup[j - 1], num[j]);
42     fd[n - 1] = F(nup[n - 1], num[0]) - // @@
43         F(nup[n - 2], num[n - 1]);
44     return fd;
45 }
```