

C++11 code 2.13.3: Sub-problem (2-13.b): Implementation of `Eval()` member function of `AnisotropicDiffusionElementMatrixProvider` for triangles → [GitLab](#)

```
2 // I. OBTAIN COORDINATES OF THE MIDPOINTS
3 // I.i Hard-code the midpoints of the edges on the reference triangle
4 Eigen::Matrix<double, 2, 3> midpoints_ref(2, 3);
5 midpoints_ref << 0.5, 0.5, 0, 0, 0.5, 0.5;
6 // I.ii Obtain the midpoints of the parametrized triangle
7 auto midpoints_param = cell_geometry->Global(midpoints_ref);
8
9 // II. COMPUTE LOCAL INTEGRATION DATA
10 // II.i Compute the inverse of the transposed Jacobian
11 //       $(J^T)^{-1} = J \star (J^T J)^{-1}$ 
12 // of the parametrization map at the midpoints of the reference triangle
13 const Eigen::MatrixXd JinvT(
14     cell_geometry->JacobianInverseGramian(midpoints_ref));
15 // II.ii Compute the integration element
16 //      integration_element(x) = sqrt(det(J^T J))
17 // where J is the Jacobian of the parametrization map
18 const Eigen::VectorXd integration_element(
19     cell_geometry->IntegrationElement(midpoints_ref));
20 // II.iii Hard-code the gradients of the reference basis functions
21 Eigen::Matrix<double, 2, 3> gradients_ref(2, 3);
22 gradients_ref << -1, 1, 0, -1, 0, 1;
23
24 // III. PERFORM NUMERICAL QUADRATURE
25 element_matrix = Eigen::MatrixXd::Zero(3, 3);
26 for (int i = 0; i < 3; i++) { // for each local degree of freedom
27     // III.i Evaluate the diffusion tensor
28     Eigen::Vector2d anisotropy_vec =
29         anisotropy_vec_field_(midpoints_param.col(i));
30     Eigen::Matrix2d diffusion_tensor =
31         Eigen::Matrix2d::Identity(2, 2) +
32         anisotropy_vec * anisotropy_vec.transpose();
33     // III. ii Compute gradients of the global basis functions
34     Eigen::MatrixXd gradients_param(2, 3);
35     gradients_param = JinvT.block(0, 2 * i, 2, 2) * gradients_ref;
36     // III. iii Compute local contribution to the element matrix
37     for (int j = 0; j < 3; j++) {
38         for (int k = 0; k < 3; k++) {
39             double integrand = (gradients_param.col(j).transpose() *
40                                 diffusion_tensor * gradients_param.col(k));
41             element_matrix(j, k) += integration_element(i) * integrand;
42         }
43     }
44 }
45 element_matrix *= 1. / 6.;
46 break;
```