

C++ code 2.4.15: Implementation of `solveA()` → [GitLab](#)

```
2 template <typename FUNCTOR1, typename FUNCTOR2>
3 Eigen::VectorXd solveA(const Eigen::VectorXd &mesh, FUNCTOR1 &&gamma,
4                       FUNCTOR2 &&f) {
5     // Nodes are indexed as 0=x_0 < x_1 < ... < x_N = 1
6     // Note: What is called N here, is M in the project description!
7     unsigned N = mesh.size() - 1;
8     // Initializations (notice initialization with zeros here)
9     Eigen::VectorXd u = Eigen::VectorXd::Zero(N + 1); // solution vec
10    Eigen::SparseMatrix<double> A(N + 1, N + 1); // laplacian galerkin mat
11    Eigen::SparseMatrix<double> M(N + 1, N + 1); // mass galerkin mat
12    Eigen::SparseMatrix<double> L(N + 1, N + 1); // full galerkin mat
13
14    // I. Build the (full) Galerkin matrix L for the lin. sys.
15    // I.i Compute the entries of the Laplace Galerkin matrix A
16    // (const. coeff. func. alpha = 1.0)
17    std::vector<Eigen::Triplet<double>> triplets_A =
18        computeA(mesh, []((double) -> double { return 1.0; }));
19    // I.ii Compute the entries of the mass matrix M
20    std::vector<Eigen::Triplet<double>> triplets_M = computeM(mesh, gamma);
21    // I.iii Assemble the sparse matrices
22    A.setFromTriplets(triplets_A.begin(), triplets_A.end());
23    M.setFromTriplets(triplets_M.begin(), triplets_M.end());
24    L = A + M; // Full Galerkin matrix of the LSE \Label[line]{SAApM}
25
26    // II. Build the right hand side source vector
27    Eigen::VectorXd rhs_vec = computeRHS(mesh, f);
28
29    // III. Enforce (zero) dirichlet boundary conditions
30    // The B.C. are  $u(0) = u(N) = 0$ . The boundary nodes are indexed by 0
31    // and N. We can therefore opt for the option of dropping first and last rows
32    // and columns of L, along with the first and last entries of the rhs_vec.
33    Eigen::SparseMatrix<double> L_reduced = L.block(1, 1, N - 1, N - 1);
34    Eigen::VectorXd rhs_vec_reduced = rhs_vec.segment(1, N - 1);
35
36    // IV. Solve the LSE  $L*u = rhs\_vec$  using an Eigen solver
37    Eigen::SimplicialLDLT<Eigen::SparseMatrix<double>, Eigen::Lower> solver;
38    solver.compute(L_reduced);
39    if (solver.info() != Eigen::Success) {
40        throw std::runtime_error("Could not decompose the matrix");
41    }
42    u.segment(1, N - 1) = solver.solve(rhs_vec_reduced);
43
44    // The solution vector u was initialized with zeros, and therefore already
45    // contains the zero Dirichlet boundary data in the first and last entry
46    return u;
47 }
```