

C++ code 2.4.25: Implementation of `solveB()` → [GitLab](#)

```
2 template <typename FUNCTOR1, typename FUNCTOR2>
3 Eigen::VectorXd solveB(const Eigen::VectorXd &mesh, FUNCTOR1 &&alpha,
4                       FUNCTOR2 &&f, double u0, double u1) {
5     // Nodes are indexed as 0=x_0 < x_1 < ... < x_N = 1
6     unsigned N = mesh.size() - 1;
7     // Initializations
8     Eigen::VectorXd u(N + 1); // solution vec
9     Eigen::SparseMatrix<double> A(N + 1, N + 1); // laplacian galerkin mat
10    // Some tool variables
11    double dx_left, dx_right; // cell widths
12
13    // I. Build the Galerkin matrix A
14    std::vector<Eigen::Triplet<double>> triplets = computeA(mesh, alpha);
15    A.setFromTriplets(triplets.begin(), triplets.end());
16
17    // II. Build the right hand side source vector
18    Eigen::VectorXd rhs_vec = computeRHS(mesh, f);
19
20    // III. Enforce dirichlet boundary conditions
21    // Proceeding as in solveA, we begin by dropping the first and last rows
22    // and columns of the galerkin matrix. The rhs_vec needs to be modified to
23    // account for the non-homogenous Dirichlet boundary conditions. It is
24    // modified using an offset function.
25    Eigen::SparseMatrix<double> A_reduced = A.block(1, 1, N - 1, N - 1);
26    Eigen::VectorXd rhs_vec_reduced = rhs_vec.segment(1, N - 1) -
27                                     A.block(1, 0, N - 1, 1) * u0 -
28                                     A.block(1, N, N - 1, 1) * u1;
29
30    // IV. Solve the LSE A*u = rhs_vec using an Eigen solver
31    Eigen::SimplicialLDLT<Eigen::SparseMatrix<double>> solver;
32    solver.compute(A_reduced);
33    if (solver.info() != Eigen::Success) {
34        throw std::runtime_error("Could not decompose the matrix");
35    }
36    u.segment(1, N - 1) = solver.solve(rhs_vec_reduced);
37
38    // The solution vector still needs to be supplemented with the known
39    // boundary values
40    u(0) = u0; // left boundary node
41    u(N) = u1; // right boundary node
42    return u;
43 }
```