

C++ code 3.17.7: Implementation of `volumeResiduals()` → [GitLab](#)

```
2 If::mesh::utils::CodimMeshDataSet<double> volumeResiduals(
3     const dataDiscreteBVP &disc_bvp, const Eigen::VectorXd & /*u_vec*/) {
4     // Get pointer to underlying mesh
5     std::shared_ptr<const If::mesh::Mesh> mesh_p =
6         disc_bvp.pwlinfespace_p->Mesh();
7     // Mesh data set for returning the volume residuals
8     If::mesh::utils::CodimMeshDataSet<double> vol_res(mesh_p, 0, 0.0);
9
10    // Edge midpoint quadrature rule for triangles, which is exact for
11    // quadratic
12    // polynomials and allows the exact computation of the volume residual
13    // contributions for piecewise linear source functions.
14    const If::quad::QuadRule qr{If::quad::make_TriaQR_EdgeMidpointRule()};
15    const Eigen::VectorXd qw{qr.Weights()}; // quadrature weight vector
16
17    // Run over all cells of the mesh
18    for (const If::mesh::Entity *cell : mesh_p->Entities(0)) {
19        LF_ASSERT_MSG(cell->RefEl() == If::base::RefEl::kTria(),
20            "Implemented for triangles only");
21        // Obtain information about the shape of the cell
22        const If::geometry::Geometry &geo{*(cell->Geometry())};
23        // Determine size of triangle (length of longest edge)
24        const Eigen::MatrixXd corners{If::geometry::Corners(geo)};
25        const double h0 = (corners.col(1) - corners.col(0)).norm();
26        const double h1 = (corners.col(2) - corners.col(1)).norm();
27        const double h2 = (corners.col(0) - corners.col(2)).norm();
28        const double h_K = std::max({h0, h1, h2});
29
30        // I: Locally integrate the square of the source function
31        // Gramian determinants
32        const Eigen::VectorXd gram_dets{geo.IntegrationElement(qr.Points())};
33        // Fetch values of source function in quadrature nodes. Note that
34        // local
35        // reference coordinates have to be passed to the evaluation
36        // operator of the
37        // MeshFunction.
38        const std::vector<double> f_vals{disc_bvp.mf_f>(*cell, qr.Points())};
39        // Evaluation of quadrature formula
40        double f_sq_int = 0.0;
41        for (If::base::size_type l = 0; l < qr.NumPoints(); ++l) {
42            f_sq_int += qw[l] * f_vals[l] * f_vals[l] * gram_dets[l];
43        }
44        // II: Fetch prefactor depending on diffusion coefficient
45        // We need a "dummy point" in the reference element in order to call
46        // the
47        // evaluation operator for the MeshFunction.
48        const Eigen::MatrixXd dummy = Eigen::Vector2d(1.0 / 3.0, 1.0 / 3.0);
49        const double alpha_K = disc_bvp.mf_alpha>(*cell, dummy)[0];
50        LF_ASSERT_MSG(alpha_K > 0,
51            "Diffusion coefficients must be strictly positive!");
52        const double mu_K = h_K * h_K / alpha_K;
53        // Store cell contribution
54        vol_res(*cell) = f_sq_int * mu_K;
55    }
56    return vol_res;
57 }
```