

C++ code 3.17.8: Implementation of `edgeResiduals()` → [GitLab](#)

```
2  If::mesh::utils::CodimMeshDataSet<double> edgeResiduals(
3      const dataDiscreteBVP &disc_bvp, const Eigen::VectorXd &u_vec) {
4      // Get pointer to underlying mesh
5      std::shared_ptr<const If::mesh::Mesh> mesh_p =
6          disc_bvp.pwlinfespace_p->Mesh();
7      // Mesh data set for returning the volume residuals
8      If::mesh::utils::CodimMeshDataSet<double> edge_res(mesh_p, 1, 0.0);
9      // Step I: Create an auxiliary MeshDataSet storing non-normalized (!)
10         edge
11         // normals = edge direction vectors turned by 90 degrees
12         If::mesh::utils::CodimMeshDataSet<Eigen::Vector2d> edge_normals(mesh_p, 1);
13         If::mesh::utils::CodimMeshDataSet<Eigen::Vector2d> edge_startpt(mesh_p, 1);
14         for (const If::mesh::Entity *edge : mesh_p->Entities(1)) {
15             // Obtain information about the shape of the edge
16             const If::geometry::Geometry &geo{*(edge->Geometry())};
17             const Eigen::MatrixXd corners{If::geometry::Corners(geo)};
18             // Starting point of the edge
19             edge_startpt(*edge) = corners.col(0);
20             // Direction vector of the edge
21             const Eigen::Vector2d dir = corners.col(1) - corners.col(0);
22             // Rotate counterclockwise by 90 degrees and store
23             edge_normals(*edge) = Eigen::Vector2d(dir(1), -dir(0));
24         }
25         // Step II: Compute the gradient of the finite element solution, which
26         // LehrFEM++ can do for us.
27         const If::fe::MeshFunctionGradFE grad_uh(disc_bvp.pwlinfespace_p, u_vec);
28
29         // Step III: Visit the triangles of the mesh, fetch the constant (!)
30         // gradient
31         // of the finite-element solution, multiply it with the edge normals
32         // and the
33         // coefficient and sum the results for every edge not located on the
34         // boundary. This summation is done in an auxiliary MeshDataSet.
35         If::mesh::utils::CodimMeshDataSet<double> alpha_max(mesh_p, 1, 0.0);
36         If::mesh::utils::CodimMeshDataSet<double> edge_flux_jump(mesh_p, 1, 0.0);
37         If::mesh::utils::CodimMeshDataSet<bool> bd_ed_flags{
38             If::mesh::utils::flagEntitiesOnBoundary(mesh_p, 1)};
39         for (const If::mesh::Entity *cell : mesh_p->Entities(0)) {
40             LF_ASSERT_MSG(cell->RefEl() == If::base::RefEl::kTria(),
41                 "Implemented for triangles only");
42             // Retrieve constant diffusion coefficient
43             const Eigen::MatrixXd dummy = Eigen::Vector2d(1.0 / 3.0, 1.0 / 3.0);
44             const double alpha_K = disc_bvp.mf_alpha_(*cell, dummy)[0];
45             LF_ASSERT_MSG(alpha_K > 0,
46                 "Diffusion coefficients must be strictly positive!");
47             // Fetch scaled gradient of the finite element solution
48             const Eigen::Vector2d nabla_u_K = (grad_uh(*cell, dummy)[0]) * alpha_K;
49             /* Debugging output
50             std::cout << "cell " << mesh_p->Index(*cell)
51                 << ": alpha*grad u_h = " << nabla_u_K.transpose() << std::endl;
52             */
53             // Obtain shape of cell
54             const If::geometry::Geometry &cell_geo{*(cell->Geometry())};
55             const Eigen::MatrixXd cell_vert{If::geometry::Corners(cell_geo)};
56             // Visit all three edges of the triangle
57             std::span<const If::mesh::Entity *const> edges{cell->SubEntities(1)};
58             LF_ASSERT_MSG(edges.size() == 3, "Triangle must have three edges!");
```