

```

2  std::vector<std::pair<unsigned int, double>> approxBoundaryFunctionalValues(
3      unsigned int L) {
4      std::vector<std::pair<unsigned int, double>> result;
5      auto meshes = generateTestMeshSequence(L - 1);
6      int num_meshes = meshes->NumLevels();
7      for (int level = 0; level < num_meshes; ++level) {
8          auto mesh_p = meshes->getMesh(level);
9
10         // Set up global FE space; lowest order Lagrangian finite elements
11         auto fe_space =
12             std::make_shared<If::uscalfe::FeSpaceLagrangeO1<double>>(mesh_p);
13
14         // Obtain local->global index mapping for current finite element
           space
15         const If::assemble::DofHandler &dofh{fe_space->LocGlobMap()};
16         const If::base::size_type N_dofs(dofh.NumDofs());
17
18         // compute galerkin matrix with alpha = 1.0, gamma = 1.0, beta = 0.0
19         auto const_one = [](Eigen::Vector2d x) -> double { return 1.0; };
20         auto const_zero = [](Eigen::Vector2d x) -> double { return 0.0; };
21         auto A = compGalerkinMatrix(dofh, const_one, const_one, const_zero);
22
23         // compute load vector for f(x) = x.norm()
24         auto f = [](Eigen::Vector2d x) -> double { return x.norm(); };
25         If::mesh::utils::MeshFunctionGlobal mf_f{f};
26         If::uscalfe::ScalarLoadElementVectorProvider elvec_builder(fe_space, mf_f);
27         Eigen::VectorXd phi(N_dofs);
28         phi.setZero();
29         AssembleVectorLocally(0, dofh, elvec_builder, phi);
30
31         // solve system of equations
32         Eigen::SparseLU<Eigen::SparseMatrix<double>> solver;
33         solver.compute(A);
34         Eigen::VectorXd u = solver.solve(phi);
35
36         // set up weight function
37         auto w = [](Eigen::Vector2d x) -> double { return 1.0; };
38         double functional_value = compBoundaryFunctional(dofh, u, w);
39
40         result.push_back({N_dofs, functional_value});
41     }
42     return result;
43 }

```