

C++ code 5.5.4: Function implementing the fixed-point iteration

```
2  template <typename FUNCTOR_F, typename RECORDER = std::function<
3          void(const Eigen::VectorXd &, double)>>
4  Eigen::VectorXd solveSemilinearBVP(
5      std::shared_ptr<const If::uscalfe::FeSpaceLagrangeO1<double>> fes_p,
6      FUNCTOR_F f, double rtol = 1.0E-4, double atol = 1.0E-8,
7      unsigned int itmax = 100,
8      RECORDER &&rec = [] (const Eigen::VectorXd &, double) -> void {} ) {
9      // Wrap right hand side source function into a Mesh Function
10     If::mesh::utils::MeshFunctionGlobal mf_f(f);
11     // Reference to current mesh
12     const If::mesh::Mesh &mesh{*(fes_p->Mesh())};
13     // Obtain local->global index mapping for current finite element space
14     const If::assemble::DofHandler &dofh{fes_p->LocGlobMap()};
15     // Dimension of finite element space
16     const std::size_t N_dofs(dofh.NumDofs());
17
18     // Assemble right-hand side vector
19     Eigen::VectorXd phi(N_dofs);
20     phi.setZero();
21     // Assemble volume part of right-hand side vector depending on the
22     source
23     // function f.
24     // Initialize object taking care of local computations on all cells.
25     If::uscalfe::ScalarLoadElementVectorProvider<double, decltype(mf_f)>
26         elvec_builder(fes_p, mf_f);
27     // Invoke assembly on cells (codim == 0)
28     If::assemble::AssembleVectorLocally(0, dofh, elvec_builder, phi);
29
30     // Coefficient vector for approximate solution
31     Eigen::VectorXd mu_vec(N_dofs);
32     // Initial guesd = 0
33     mu_vec.setZero();
34     // Main fixed-point iteration loop
35     Eigen::VectorXd mu_old(N_dofs);
36     double diff_norm; // Norm of correction
37     unsigned int steps = 0;
38     do {
39         mu_old = mu_vec;
40         // Solve linear fixed-point system and return solution in mu_vec
41         fixedPointNextIt(fes_p, mu_vec, phi);
42         diff_norm = (mu_vec - mu_old).norm();
43         rec(mu_vec, diff_norm);
44         steps++;
45         // Correction-based termination
46     } while ((diff_norm >= rtol * mu_vec.norm()) && (diff_norm >= atol) &&
47             (steps < itmax));
48     return mu_vec;
49 }
```