

C++ code 9.18.21: Implementation of `timestepDissipativeWaveEquation()`

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2  Eigen::VectorXd timestepDissipativeWaveEquation(
3      std::shared_ptr<const If::uscalfe::FeSpaceLagrangeO2<double>> fe_space_p,
4      double T, unsigned int M, Eigen::VectorXd mu0, Eigen::VectorXd nu0) {
5      // Pointer and reference to current mesh
6      std::shared_ptr<const If::mesh::Mesh> mesh_p = fe_space_p->Mesh();
7      const If::mesh::Mesh &mesh{*mesh_p};
8      // Obtain local->global index mapping
9      // for current finite element space
10     const If::assemble::DofHandler &dofh{fe_space_p->LocGlobMap()};
11     // Dimension of finite element space = number of nodes of the mesh
12     const If::base::size_type N_dofs(dofh.NumDofs());
13     LF_VERIFY_MSG(mu0.size() == N_dofs, "Wrong length of mu0");
14     LF_VERIFY_MSG(nu0.size() == N_dofs, "Wrong length of nu0");
15     // The solution vector at time T
16     Eigen::VectorXd mu = mu0;
17
18     // Obtain matrices in triplet format
19     const auto [M_COO, B_COO, A_COO] = computeGalerkinMatrices(fe_space_p);
20     LF_VERIFY_MSG((M_COO.cols() == N_dofs) && (M_COO.rows() == N_dofs),
21         "Wrong size of M");
22     LF_VERIFY_MSG((B_COO.cols() == N_dofs) && (B_COO.rows() == N_dofs),
23         "Wrong size of B");
24     LF_VERIFY_MSG((A_COO.cols() == N_dofs) && (A_COO.rows() == N_dofs),
25         "Wrong size of A");
26     // For convenience convert in CRS format in order to be able to exploit
27     // Eigen's linear-algebra operations.
28     const Eigen::SparseMatrix<double> M_crs{M_COO.makeSparse()};
29     const Eigen::SparseMatrix<double> B_crs{B_COO.makeSparse()};
30     const Eigen::SparseMatrix<double> A_crs{A_COO.makeSparse()};
31     // Build sparse matrices  $M+0.5\tau*B$  and  $M-0.5\tau*B$ 
32     // Timestep size
33     const double tau = T / M;
34     const std::vector<Eigen::Triplet<double>> &B_trp = B_crs.triplets();
35     std::vector<Eigen::Triplet<double>> MBp_trp = M_COO.triplets();
36     std::vector<Eigen::Triplet<double>> MBm_trp = M_COO.triplets();
37     for (auto &triplet : B_trp) {
38         MBp_trp.emplace_back(triplet.row(), triplet.col(),
39             0.5 * tau * triplet.value());
40         MBm_trp.emplace_back(triplet.row(), triplet.col(),
41             -0.5 * tau * triplet.value());
42     }
43     Eigen::SparseMatrix<double> MBp(N_dofs, N_dofs);
44     MBp.setFromTriplets(MBp_trp.begin(), MBp_trp.end());
45     Eigen::SparseMatrix<double> MBm(N_dofs, N_dofs);
46     MBm.setFromTriplets(MBm_trp.begin(), MBm_trp.end());
47     // We have to solve a linear system with the matrix  $M+0.5\tau*B$ 
48     Eigen::SparseLU<Eigen::SparseMatrix<double>> solver_MBp;
49     // LU decomposition, important: outside main timestepping loop
50     solver_MBp.compute(MBp);
51     LF_VERIFY_MSG(solver_MBp.info() == Eigen::Success,
52         "LU decomposition of  $M+0.5\tau*B$  failed");
53     // The auxiliary vector in the timestepping loop
54     Eigen::VectorXd nu(N_dofs);
55     // Special initial step
56     {
57         Eigen::SparseLU<Eigen::SparseMatrix<double>> solver_M;

```