

C++ code 9.8.33: Solver for nonlinear Schrödinger equation → [GitLab](#)

```
2 // Load mesh and initialize FE space and DOF handler
3 auto mesh_factory = std::make_unique<If::mesh::hybrid2d::MeshFactory>(2);
4 const If::io::GmshReader reader(std::move(mesh_factory),
5                                 "meshes/square_64.msh");
6 auto mesh_p = reader.mesh();
7 auto fe_space =
8     std::make_shared<If::uscalfe::FeSpaceLagrangeO1<double>>(mesh_p);
9 const If::assemble::DofHandler &dofh{fe_space->LocGlobMap()};
10 const If::uscalfe::size_type N_dofs(dofh.NumDofs());
11
12 // Mass matrix
13 If::assemble::COOMatrix<double> D_COO(N_dofs, N_dofs);
14 NonLinSchroedingerEquation::MassElementMatrixProvider mass_emp;
15 If::assemble::AssembleMatrixLocally(0, dofh, dofh, mass_emp, D_COO);
16 Eigen::SparseMatrix<double> D = D_COO.makeSparse();
17 Eigen::SparseMatrix<std::complex<double>> M = std::complex<double>(0, 1) * D;
18
19 // Stiffness matrix
20 If::assemble::COOMatrix<double> A_COO(N_dofs, N_dofs);
21 If::uscalfe::LinearFELaplaceElementMatrix stiffness_emp;
22 If::assemble::AssembleMatrixLocally(0, dofh, dofh, stiffness_emp, A_COO);
23 Eigen::SparseMatrix<double> A = A_COO.makeSparse();
24
25 // Prepare timestepping
26 int timesteps = 100;
27 double T = 1.0;
28 double tau = T / timesteps;
29
30 // Prepare initial data
31 const double PI = 3.14159265358979323846;
32 auto u0 = [PI](Eigen::Vector2d x) -> double {
33     return 4.0 * std::cos(PI * x(0)) * std::cos(PI * x(1));
34 };
35 If::mesh::utils::MeshFunctionGlobal mf_u0{u0};
36 Eigen::VectorXcd mu = If::fe::NodalProjection(*fe_space, mf_u0);
37
38 // Prepare split-step propagator for full step  $\tau$ 
39 NonLinSchroedingerEquation::SplitStepPropagator splitStepPropagator(A, M,
40                               tau);
41
42 // Arrays for storing "energies" contributing to the Hamiltonian
43 Eigen::VectorXd norm(timesteps + 1);
44 Eigen::VectorXd E_kin(timesteps + 1);
45 Eigen::VectorXd E_int(timesteps + 1);
46 // Timestepping
47 for (int j = 0; j < timesteps; ++j) {
48     // Compute norm and energy along the solution
49     norm(j) = NonLinSchroedingerEquation::Norm(mu, D);
50     E_kin(j) = NonLinSchroedingerEquation::KineticEnergy(mu, A);
51     E_int(j) = NonLinSchroedingerEquation::InteractionEnergy(mu, D);
52     // Timestep tau according to Strang splitting
53     mu = splitStepPropagator(mu);
54 }
55 norm(timesteps) = NonLinSchroedingerEquation::Norm(mu, D);
56 E_kin(timesteps) = NonLinSchroedingerEquation::KineticEnergy(mu, A);
57 E_int(timesteps) = NonLinSchroedingerEquation::InteractionEnergy(mu, D);
```