## Department of Pure Mathematics

Module 110PMA207 - Linear Algebra
Assignment 7

1. Plot the pairs $(x, y)$ which satisfy the equation

$$
-2 x+5 y=10
$$

2. Solve the linear equations
(a) $2 x+2 y=2$ $-2 x-4 y=8$
(b) $y=x-1$
$y=-2 x+5$
numerically as well as geometrically.
3. How many solutions has the following system of equations?

$$
\begin{aligned}
-3 x-9 y+6 z & =12 \\
x+3 y-2 z & =4
\end{aligned}
$$

4. Find all solution to the following system of equations:

$$
\begin{aligned}
x_{1}+x_{2}+x_{3}+x_{4} & =1 \\
x_{1}+2 x_{2}+4 x_{3}+8 x_{4} & =-1 \\
x_{1}+3 x_{2}+9 x_{3}+27 x_{4} & =-1 \\
x_{1}+4 x_{2}+16 x_{3}+64 x_{4} & =1
\end{aligned}
$$

5. Find all solution to the following system of equations:

$$
\begin{aligned}
& x_{1}+2 x_{2}+3 x_{3}+4 x_{4}=4 \\
& 2 x_{1}+3 x_{2}+4 x_{3}+x_{4}=-12 \\
& 2 x_{1}+x_{2}+2 x_{3}+5 x_{4}=16 \\
& 4 x_{1}+x_{2}+2 x_{3}+3 x_{4}=12
\end{aligned}
$$

Hint: Notice that the rank of the corresponding matrix is 3 (which implies that the solution cannot be unique).

