Department of Pure Mathematics

Module 110PMA207 - Linear Algebra

Assignment 7

1. Plot the pairs (x, y) which satisfy the equation

$$-2x + 5y = 10$$

2. Solve the linear equations

(a)
$$2x + 2y = 2$$

 $-2x - 4y = 8$

(b)
$$y = x - 1$$

 $y = -2x + 5$

numerically as well as geometrically.

3. How many solutions has the following system of equations?

$$-3x - 9y + 6z = 12$$

 $x + 3y - 2z = 4$

4. Find all solution to the following system of equations:

$$x_1 + x_2 + x_3 + x_4 = 1$$

$$x_1 + 2x_2 + 4x_3 + 8x_4 = -1$$

$$x_1 + 3x_2 + 9x_3 + 27x_4 = -1$$

$$x_1 + 4x_2 + 16x_3 + 64x_4 = 1$$

5. Find all solution to the following system of equations:

$$\begin{array}{rcl} x_1 + 2x_2 + 3x_3 + 4x_4 & = & 4 \\ 2x_1 + 3x_2 + 4x_3 + x_4 & = & -12 \\ 2x_1 + x_2 + 2x_3 + 5x_4 & = & 16 \\ 4x_1 + x_2 + 2x_3 + 3x_4 & = & 12 \end{array}$$

Hint: Notice that the rank of the corresponding matrix is 3 (which implies that the solution cannot be unique).